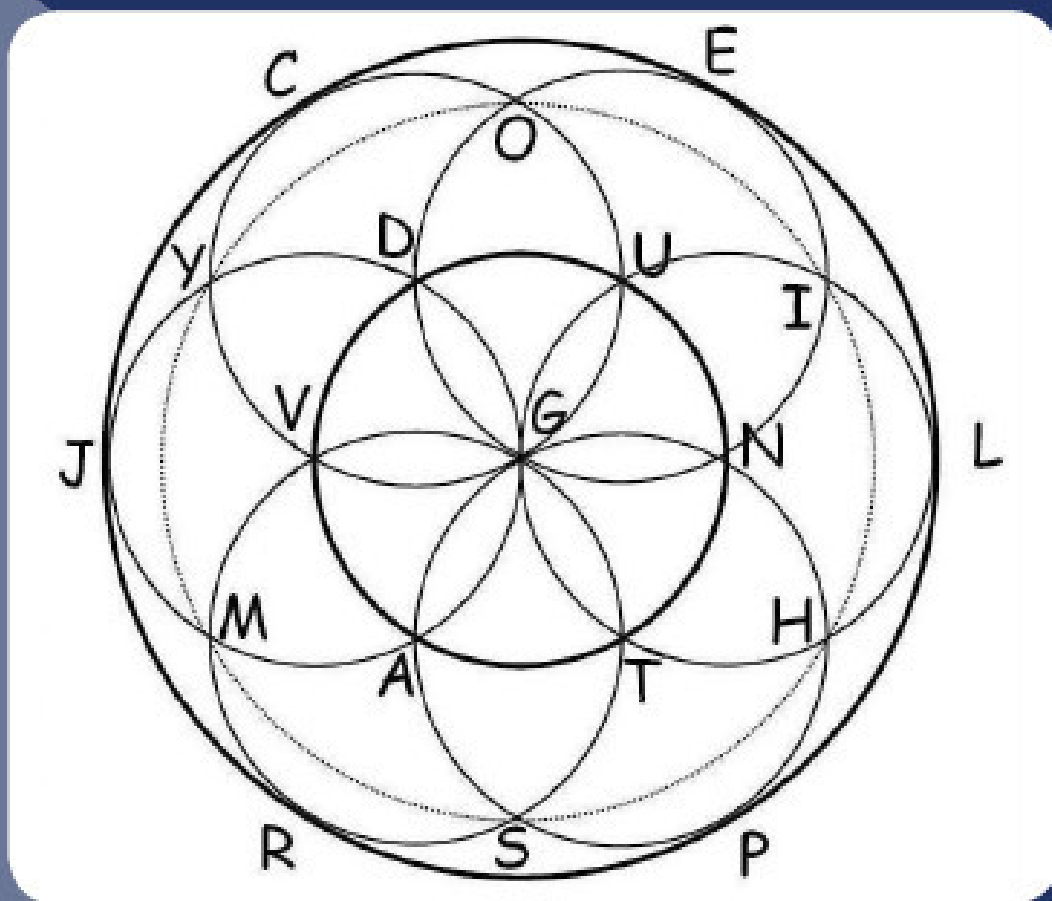


Twenty Problem Solving Skills

FOR MATHCOUNTS
COMPETITIONS



JANE CHEN

Twenty Problem Solving Skills For Mathcounts Competitions

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This book is dedicated to Dr. Harold Reiter, who opened the door to the world of mathematics for me, who has always been there for me, and who inspired me to write this book.

About the Author

Jane Chen has been an avid math competitor ever since elementary school. She qualified for American Invitational Mathematics Exam (AIME) when she was nine years old.

She was a

USA Math Olympiad Qualifier (2009, 2010)

AIME top scorer among all girls across the US (2009 and 2010)

AMC 12 top scorer among all girls across the US (2010)

AMC 10 Perfect Scorer (2007, 2009)

MATHCOUNTS Nationals Alumni (2007)

Canadian Math Olympiad Qualifier (2008)

Massachusetts Math Olympiad Finalist (2008, 2009)

She is a senior at Phillips Academy Andover.

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